Coherent modulation of the YBa$_2$Cu$_3$O$_{6+x}$ atomic structure by displaceable stimulated ionic Raman scattering

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We discuss the mechanism of coherent phonon generation by stimulated ionic Raman scattering, a process different from conventional excitation with near visible optical pulses. Ionic Raman scattering is driven by anharmonic coupling between a directly excited infrared-active phonon mode and other Raman modes. We experimentally study the response of YBa$_2$Cu$_3$O$_{6+x}$ to the resonant excitation of apical oxygen motions at 20 THz by midinfrared pulses, which has been shown in the past to enhance the interlayer superconducting coupling. We find coherent oscillations of four totally symmetric ($\lambda_I$) Raman modes and make a critical assessment of the role of these oscillatory motions in the enhancement of superconductivity.

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Midinfrared light pulses can be used to resonantly excite optically active lattice vibrations in solids to amplitudes as high as several percent of interatomic distances. This technique has been shown to induce changes in the collective magnetic and electronic properties of many materials [1–3]. Integral to this optical control mechanism is the anharmonic coupling between the directly driven, optically active mode and other lattice vibrations [4–6]. The coupling is typically dominated by cubic anharmonicities and involves a displaceable force that acts onto the crystal lattice in two ways.

First, a phononic analog to rectification in nonlinear optics causes a quasistatic displacement along the normal mode coordinates of all coupled Raman modes. Secondly, whenever the displaceable force rises promptly compared to the period of any of the anharmonically coupled modes, coherent oscillatory motions of these modes are excited. This second effect is the stimulated equivalent of ionic Raman scattering.

Here, we study the coherent optical response of YBa$_2$Cu$_3$O$_{6+x}$. Infrared-active apical oxygen motions are driven resonantly with midinfrared pulses at 20 THz, under the conditions for which superconducting transport is transiently enhanced [7–9]. We find that for excitation with pulses of 140 fs duration, for which only modes with frequency < 6 THz can be driven coherently, oscillations of four Raman modes are stimulated, involving displacements of the copper atoms along the crystallographic c axis. This motion induces periodic changes in the in-plane O-Cu bond buckling and leads to an oscillatory transfer of charges between the CuO$_2$ planes and the Cu-O chains [9], effectively modifying the doping of the planes; an effect that may be part of the puzzle of optically enhanced superconductivity in this compound [7–9].

We next discuss the process of stimulated ionic Raman scattering in more detail. The indirect excitation of coherent Raman modes by resonant excitation of large amplitude infrared-active (IR) vibrations in a solid is described to lowest order by the lattice Hamiltonian

$$H = \frac{1}{2}\omega_{IR}^2 Q_{IR}^2 + \frac{1}{2}\omega_{R}^2 Q_{R}^2 - a_{12} Q_{IR} Q_{R}^2 - a_{21} Q_{IR}^2 Q_{R}. \quad (1)$$

where $(\omega_{IR}, Q_{IR})$ and $(\omega_{R}, Q_{R})$ denote the respective frequency and normal coordinates of the directly excited IR mode and of any anharmonically coupled mode. In this equation, $a_{12}$ and $a_{21}$ are the coupling constants. For centrosymmetric crystals like YBa$_2$Cu$_3$O$_{6+x}$, the term $a_{12} Q_{IR} Q_{R}^2$ is forbidden as any infrared mode $Q_{IR}$ is odd (breaks inversion symmetry), whereas $Q_{R}^2$ is even (conserves inversion symmetry). Furthermore, $Q_{IR}$ in $a_{12} Q_{IR}^2 Q_{R}$ must be a Raman mode as $Q_{IR}^2$ is even. The Hamiltonian thus reduces to

$$H = \frac{1}{2}\omega_{IR}^2 Q_{IR}^2 + \frac{1}{2}\omega_{R}^2 Q_{R}^2 - a_{21} Q_{IR}^2 Q_{R}. \quad (2)$$

The corresponding dynamical response of the modes is described by the equations of motion

$$\ddot{Q}_{IR} + 2\gamma_{IR} \dot{Q}_{IR} + \omega_{IR}^2 Q_{IR} = f(t) + 2a_{21} Q_{IR} Q_{R}. \quad (3)$$

$$\ddot{Q}_{R} + 2\gamma_{R} \dot{Q}_{R} + \omega_{R}^2 Q_{R} = a_{21} Q_{IR}^2. \quad (4)$$

Dissipation is accounted for by the terms containing $\gamma$, which is the inverse lifetime of the respective phonon mode $\gamma = \tau^{-1}$. The equation for the IR mode $Q_{IR}$ describes a damped harmonic oscillator driven by the electric field of the midinfrared pulse $f(t) = A(t)e^{i\omega_{IR}t}$, with $A(t)$ being the Gaussian envelope of the pulse. Upon excitation, the atoms perform oscillations along the IR mode eigenvector about their equilibrium positions as shown in Fig. 1(a) in light red. This motion, for a finite anharmonic coefficient $a_{21}$, exerts a directional force $F(t) = a_{21} Q_{IR}^2(t)$ proportional to $Q_{IR}^2$ onto the coupled Raman mode [Fig. 1(b)].

Hence, the atoms experience a displacement along all coupled Raman-mode eigenvectors. This displacement may occur fast or slow compared to the eigenfrequency of each coupled mode. The lattice relaxes back to equilibrium over a time scale that is one-half of the dephasing time of the infrared mode $\tau_{IR} = 1/\gamma_{IR}$ assuming no transition into a metastable state takes place. The one-half factor for the relaxation time descends from the fact that the squared amplitude of the IR mode appears in the driving term in Eq. (4). This effect has been studied in detail in Refs. [6] and [9].
apical oxygen atoms between these bilayers at vacant chains sites only, or between oxygenvacancy. insulating yttrium layer. Holes are doped in these planes by changing the oxygen content of Cu-O chains, which are alternat ingly filled and empty in the ortho-II ordered structure of YBa$_2$Cu$_3$O$_{6+x}$ for $x = 0.5$ or 0.55. The resonantly excited $B_{1u}$ mode consists of movements of the apical oxygen atoms between these bilayers at chain sites with an oxygen vacancy.

Secondly, as discussed in the introduction, the coupled Eqs. (3) and (4) predict that all of the displaced modes, which have a long enough eigenperiod, will exhibit coherent oscillations about the displaced atomic positions. Specifically, this happens only for those modes with eigenperiod $T_R$ long compared to the rise time of the directional force, or, equivalently, compared to the width of the midinfrared pulse envelope $\Delta_{IR}$ driving the odd mode $Q_{IR}$. The precise oscillation amplitude will further depend on the anharmonic coupling constant but also on the rise and decay times of the driving force $F(t)$ compared to the eigenperiod of the Raman mode. This is again captured by the two classical equations of motion. Further, unlike for the displacive response discussed above, these oscillations relax over a time scale that is determined by the lifetime of the Raman mode $\tau_R = 1/\gamma_R$, which may be far longer than $\tau_{IR}/2$ (see blue and red oscillations in Fig. 1).

Finally, the phase of the oscillations may be zero or finite, depending on whether the process is in the impulsive or displacive limit. In the impulsive limit ($T_R \gg \Delta_{IR}$, $\tau_R$ and $\omega_{IR} \gg \omega_R$), the infrared-active mode decays back to its ground state before the Raman mode has started oscillating. Hence, Raman oscillations take place about the equilibrium lattice coordinates, with $Q_R(t) \sim \sin(\omega_R t)$. In the displacive limit ($T_R \gg \Delta_{IR}$, $T_R \ll \tau_{IR}$, and $\omega_{IR} \gg \omega_R$), the IR mode and the displacive response decay slowly, and the Raman excitation occurs about the displaced positions. The force $F(t)$ acting on the Raman mode can be approximated by a step function and $Q_R(t) \sim [1 - \cos(\omega_R t)]$. In most cases, the oscillations will have a phase that is neither sine nor cosine, or the phase of the Raman mode may change over time [10].

For conventional electronic stimulated Raman scattering, the equation of motion [Eq. (4)] has the same structure and the same limits discussed above can be derived [11,12]. The physical process is, however, fundamentally different, as in conventional stimulated Raman scattering the driving force derives from electronic transitions [13]. On the contrary, in ionic stimulated Raman scattering the driving force solely depends on lattice variables [14–17]. The excitation process is therefore most sensitive to phase transitions that affect the lattice.

In the following, we discuss experiments performed on YBa$_2$Cu$_3$O$_{6.5}$ and YBa$_2$Cu$_3$O$_{6.55}$, two bilayer high-temperature superconductors with a critical temperature of $T_c = 50$ K and $T_c = 61$ K, respectively. These two compounds crystallize in a centrosymmetric orthorhombic structure with $D_{2h}$ symmetry. The bilayers comprise two conducting CuO$_2$ layers in the $ab$ plane, which are separated by an insulating yttrium layer [Fig. 1(c)]. The CuO$_2$ planes are hole doped by adding oxygen atoms to the Cu-O chains along the $b$ axis, which are vacant of oxygen atoms in the parent compound YBa$_2$Cu$_3$O$_6$. The samples measured in this work exhibited ortho-II ordering of the oxygen atoms, corresponding to a structure for which alternate Cu-O chains are filled and empty. The YBa$_2$Cu$_3$O$_{6.5}$ sample exhibited only short-range ordered domains, whereas the YBa$_2$Cu$_3$O$_{6.55}$ samples showed long-range ordering of these chains [18].

In samples with these doping levels, the resonantly excited $B_{1u}$ symmetry mode at $20$ THz consists of movements of the apical oxygen atoms between bilayers at vacant chain sites only [blurred motion in Fig. 1(c)] [19]. The long-range ordering of the chain vacancies in the YBa$_2$Cu$_3$O$_{6.55}$ sample might...
therefore influence the structural dynamics. According to the symmetry argument discussed above, nonlinear coupling is restricted to modes of $A_g$ symmetry as the product group of $B_{1u}$ with itself as $A_g$. We thus expect a transient displacement of the crystal lattice along all of these modes with finite anharmonic coupling. Because atomic motions along Raman coordinates modulate the polarizability tensor, these motions become observable as changes in the reflectivity of the material. We used 140 fs mid-infrared pulses (15 μm, 10% bandwidth) with a fluence of 2.5 mJ/cm$^2$ to drive the sample into its transient state, and probed the reflection of 35 fs pulses at 800 nm wavelength. Under this condition, we expect the excitation of modes up to $\sim 6$ THz in frequency. According to their Raman tensor for the orthorhombic $D_{2h}$ point group, the $A_g$ Raman modes are observable but have different tensor elements for probe polarizations in plane along $a$ and $b$, as well as out of plane along the $c$ direction [20].

The experimental results, reported for both out-of-plane and in-plane polarized probe pulses, are shown in Fig. 2(a) for YBa$_2$Cu$_3$O$_{6.55}$. The oscillatory response was obtained by subtracting a fit to the data consisting of an error function and a triple-exponential decay (thin black line) and is shown in the inset for 10 K sample temperature. While sign and size of the total response are different for the two orthogonal polarizations, we find no difference between the amplitudes and absolute phases of the oscillations.

For YBa$_2$Cu$_3$O$_6$ and YBa$_2$Cu$_3$O$_{6.5}$, we find three dominant frequency components [Figs. 2(b) and 2(c)], which can be attributed to four $A_g$ phonon modes ($A_{g14}$, $A_{g15}$, $A_{g21}$, and $A_{g29}$) [9] that are shown in Fig. 3(a). The numbers denote the index of the respective phonon modes, as sorted according to their frequencies. We find no significant differences in the response to the excitation between the two samples. We stress that these modes could not be detected in the x-ray experiments of Ref. [9], as the signal to noise ratio was not sufficiently high.

Note that these oscillatory modes were also observed in YBa$_2$Cu$_3$O$_{6.9}$ after excitation with 2 eV pulses [21–23]. In these experiments, large changes were found in the relative amplitudes of these modes and relaxation dynamics when crossing the critical temperature $T_c$, as the excitation mechanism relied on optical transitions between electronic states that strongly change through the superconducting transition. Here, we only find a continuous increase in both phonon amplitudes and nonoscillatory components upon decreasing temperature, as only small changes in the equilibrium infrared phonon spectrum take place at $T_c$.

The observed oscillations at 2.6, 3.8, and 4.6 THz in YBa$_2$Cu$_3$O$_{6.55}$ are shown in Fig. 2(d), displaying a clear cosine phase at time zero (black line; gray area is the uncertainty), indicative of a dispersive rather than an impulsive mechanism ($\tau_R \ll \tau_{IR}$). This relation can be validated by estimating the relaxation time of the IR mode $\tau_{IR}$ from the decay time of the
atomic displacements $\tau_D$, which has been measured by x-ray diffraction and reported in Ref. [9], by $\tau_{IR} = 2\tau_D$. We obtain a relaxation time $\tau_{IR} = 2.4$ ps, which is larger by factors of 11, 9, and 6 compared to the periods of the observed oscillations at 2.6, 3.8, and 4.6 THz, respectively, consistent with a displacive excitation. We can attribute these oscillations to the four lowest frequency $A_g$ modes of the ortho-II ordered YBa$_2$Cu$_3$O$_{6+x}$ structure. From the presented data alone, the amplitudes of the atomic motions cannot be quantified, as the changes in the electronic polarizability at 800 nm may be different for each mode and are not known here [13].

We obtain a qualitative estimate of the real-space amplitudes by starting from the measurements of the underlying rectified displacement by ultrafast hard x-ray diffraction of Ref. [9]. For the 140 fs midinfrared pulses used to drive the odd apical oxygen mode, the relative amplitude of oscillatory and displacive responses only depends on the Raman mode frequency and can be calculated from Eqs. (3) and (4) [Fig. 3(b)]. From these calculations and the displacement amplitudes $\Delta d_{\text{Displ}}$ of the four $A_g$ modes, we estimate the oscillatory amplitudes $\Delta d_{\text{Osc}}$ of the respective vibrations for the same fluence of Refs. [7–9] of 4 mJ/cm$^2$ by $\Delta d_{\text{Osc}} = \Delta d_{\text{Displ}}(\Delta Q_{\text{Osc}}/\Delta Q_{\text{Displ}})$ (see Table I). The atomic motions of these modes [Fig. 3(a)] are dominated by a change in distance between Cu atoms of neighboring CuO$_2$ planes along the crystallographic $c$ axis [Fig. 4(a)]. We estimate oscillation amplitudes in these distances of $\sim 0.9$ and $\sim 0.5$ pm at vacant ($d_1$) and filled ($d_2$) chain sites, relaxing with a decay time of 3 ps, as shown in Fig. 4(b).

At this stage we can speculate if the phenomenon of enhanced interlayer coupling, sometimes referred to as light-induced superconductivity, may or may not be connected to these oscillations. According to the calculations of Ref. [9], the oscillatory motions reported above will couple to the density of states of the $d^3$ Cu orbitals in the chains and the planar Cu $d_{x^2−y^2}$ orbitals, and induce a charge transfer between plane and chain. We speculate here that these oscillations will modulate the interlayer tunneling and with it the coupling between the planes. The full dynamics shown in Fig. 4(c), which includes the displacive response, decreases the distances between plane and chain, and forces a net charge transfer from the planar Cu to the chain Cu, effectively increasing the hole doping of the planes. This charge transfer is emerging as a key process in the formation of superconductivity, as shown, for instance, by the self-doping effect recently found to accompany the temperature-driven metal-superconductor phase transition in YBa$_2$Cu$_3$O$_{6.9}$ [24].

In a recent theoretical paper [25], we showed how modulation of the interlayer couplings may cause a reduction and parametric cooling of phase fluctuations, an effect that may aid superconductivity in the driven state. We found that this effect is strongest for modulations at the difference frequency between the intrabilayer and interbilayer Josephson plasmon, which in YBa$_2$Cu$_3$O$_{6.5}$ are at $\sim 13$ and $\sim 1$ THz, respectively. The modulations detected here are strongest at $\sim 4$ THz, and cannot account for such parametric cooling directly. For this

![FIG. 3. (Color online) (a) Four lowest frequency $A_g$ modes of the ortho-II ordered YBa$_2$Cu$_3$O$_{6+x}$ structure [9]. (b) Calculated ratio between oscillation and displacement amplitude of the five lowest frequency $A_g$ phonon modes after excitation of the $B_{1u}$ infrared mode with 140 fs midinfrared pulses.](image)

<table>
<thead>
<tr>
<th>$A_g$</th>
<th>$\Delta d_{1\text{Displ}}$ (pm)</th>
<th>$\Delta d_{2\text{Displ}}$ (pm)</th>
<th>Frequency (THz)</th>
<th>$\Delta Q_{\text{Osc}}/\Delta Q_{\text{Displ}}$</th>
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<tbody>
<tr>
<td>$A_{14}$</td>
<td>0.29</td>
<td>$-0.30$</td>
<td>2.80</td>
<td>0.64</td>
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<tr>
<td>$A_{15}$</td>
<td>0.81</td>
<td>0.76</td>
<td>2.83</td>
<td>0.64</td>
</tr>
<tr>
<td>$A_{21}$</td>
<td>0.73</td>
<td>0.63</td>
<td>3.85</td>
<td>0.40</td>
</tr>
<tr>
<td>$A_{29}$</td>
<td>0.24</td>
<td>$-0.34$</td>
<td>4.59</td>
<td>0.24</td>
</tr>
</tbody>
</table>
FIG. 4. (Color online) (a) The combined atomic motions of the $A_g$ modes primarily involve $c$-axis movement of the planar Cu atoms. To describe the structural dynamics, we define $d_1$ and $d_2$ as the distances between Cu atoms (large blue spheres) of neighboring CuO$_2$ planes at vacant and filled chain sites, respectively. (b) Changes in these distances due to excitation of the $A_g$ phonon modes. We estimate oscillation amplitudes of 0.9 and 0.5 pm in $d_1$ and $d_2$, with a relaxation time of 3 ps. (c) The full dynamics including the displacive response involve an increase in both $d_1$ and $d_2$ accompanied by oscillations.

...effect to be effective the coupling would have to occur at the third harmonic frequency of the modulation, an effect that is unlikely but not impossible. Yet, we cannot exclude that modes may cause dynamical stabilization of interlayer fluctuations by other, related mechanisms different from the parametric cooling of Ref. [25], which may involve modulations of the electronic properties [26].

In summary, we have studied coherent phonon generation by displacive stimulated ionic Raman scattering in YBa$_2$Cu$_3$O$_{6.5}$ and YBa$_2$Cu$_3$O$_{6.55}$. We have reported measurements of coherent oscillations of four $A_g$ phonon modes, triggered by anharmonically coupled apical oxygen motions, directly driven by midinfrared pulses. This excitation is significant because in other experiments it has been shown to enhance superconducting interlayer tunneling. We present a model describing the generation mechanism based on cubic coupling of a directly driven infrared mode to other Raman modes. We combine this model with results of previous ultrafast x-ray diffraction experiments to estimate the oscillatory atomic motions and their amplitudes. We propose that the motions modulate the interlayer tunneling between adjacent CuO$_2$ planes, which may contribute to promoting superconductivity by periodic modulation of the Hamiltonian parameter.

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