

## Pressure-Dependent Relaxation in the Photoexcited Mott Insulator ET-F<sub>2</sub>TCNQ: Influence of Hopping and Correlations on Quasiparticle Recombination Rates

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We measure the ultrafast recombination of photoexcited quasiparticles (holon-doublon pairs) in the one dimensional Mott insulator ET-F<sub>2</sub>TCNQ as a function of external pressure, which is used to tune the electronic structure. At each pressure value, we first fit the static optical properties and extract the electronic bandwidth  $t$  and the intersite correlation energy  $V$ . We then measure the recombination times as a function of pressure, and we correlate them with the corresponding microscopic parameters. We find that the recombination times scale differently than for metals and semiconductors. A fit to our data based on the time-dependent extended Hubbard Hamiltonian suggests that the competition between local recombination and delocalization of the Mott-Hubbard exciton dictates the efficiency of the recombination.

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The recombination of hot carriers in solids is a fundamental process of interest to nonlinear optics and to device applications, as well as a spectroscopic tool that exposes the physics of interacting microscopic degrees of freedom. “Hot electron” spectroscopy has been applied extensively to metals and semiconductors, for which well-established models have been developed.

For direct gap semiconductors recombination occurs at a rate that depends on the joint density of states between valence and conduction bands  $\propto (\partial E_v / \partial k)(\partial E_c / \partial k)$ , and is thus expected to *slow down* with the square of the bandwidth  $\tau \propto t^2$ . On the other hand, in the case of metals, the dynamics are well captured by the two-temperature model [1,2], which considers the energy stored in the optically excited nonequilibrium electron distribution as flowing into the lattice at a rate determined by the electron-phonon coupling strength and by the electronic and lattice heat capacities. As the relaxation of hot electrons accelerates with smaller electronic specific heat, and because  $c_v^e$  is proportional to the density of states at the Fermi level [3], for metals relaxation should accelerate linearly with the reciprocal of the bandwidth  $\tau \propto 1/t$ .

For solids with strongly correlated electrons, the dependence of nonequilibrium quasiparticle recombination rates on the microscopic parameters has not been systematically

investigated and it is not well understood. In this Letter, we study the recombination of impulsively excited quasiparticles in a one dimensional Mott insulator, in which we tune electronic bandwidth and intersite correlation energy by applying external pressure. We find that the recombination of quasiparticles accelerates for increasing bandwidth, as expected for a metal, but with a dependence on microscopic parameters that is unique to the physics of electronic insulators in one dimension and that descends from a competition between local decay and coherent delocalization of photoexcited holon-doublon pairs [4].

We study bis-(ethyldithio)-tetrathiafulvalene-difluorotetracyano-quinodimethane (ET-F<sub>2</sub>TCNQ), a half filled organic salt with quasi-1D electronic structure, negligible electron-phonon interaction [5], and with electronic properties that are well captured by a 1D extended Hubbard model [4,6]

$$H = -t \sum_{j\sigma} (\hat{c}_{j\sigma}^\dagger \hat{c}_{j+1\sigma} + \text{H.c.}) + V \sum_j \hat{n}_j \hat{n}_{j+1} + U \sum_j \hat{n}_{j\uparrow} \hat{n}_{j\downarrow}. \quad (1)$$

Our experiments were performed under external pressure, which reduces the lattice spacing between the molecular sites and tunes the hopping amplitude ( $t$ ) and repulsion

(attraction) between electron (electron-hole) pairs on neighboring sites ( $V$ ). In the simplified case of hydrogenic wave functions in one dimension [7,8],  $t$  depends exponentially on the lattice spacing  $R$  as  $t(R) \propto (1 + \alpha R)e^{-\alpha R}$ . The decrease in the lattice spacing  $R$  results then in an increase of the intersite Coulomb repulsion  $V$  as  $V(R) \propto e^2/R$  [9]. Within these simplifying assumptions, the onsite Coulomb interaction  $U$ , which is determined by the local electronic properties of the molecular sites, is considered independent on the lattice spacing [10].

For calibration, we first measured and fitted the static optical properties as a function of pressure (see Supplemental Material [11]). In Fig. 1, we report the reflectivity measured at 300 K for electric field polarized along the 1D charge transfer direction ( $a$  axis). The corresponding optical conductivity  $\sigma_1(\omega)$  was extracted by a Kramers-Kronig consistent fit. At ambient conditions [see Figs. 1(a) and (b)],  $\sigma_1(\omega)$  exhibits a prominent peak near 700 meV, indicative of electron-electron correlations and of a Mott gap [5]. As pressure was applied, the 700 meV charge transfer (CT) resonance was observed to shift to the red at a rate of 70 meV/GPa, broadening toward high frequencies [see Figs. 1(c) and (d)]. This pressure dependence is consistent with the behavior measured previously in other quasi-1D compounds [12,13]. For all measured photon energies ( $>75$  meV), no Drude response was observed at any pressure (0–2 GPa), indicating that the material remains insulating and one dimensional [13,14]. The vibrational peaks at frequencies below 400 meV exhibited no pressure dependence, excluding significant intramolecular structural rearrangement.

The data were analyzed using a model of the optical conductivity based on the extended Hubbard Model of

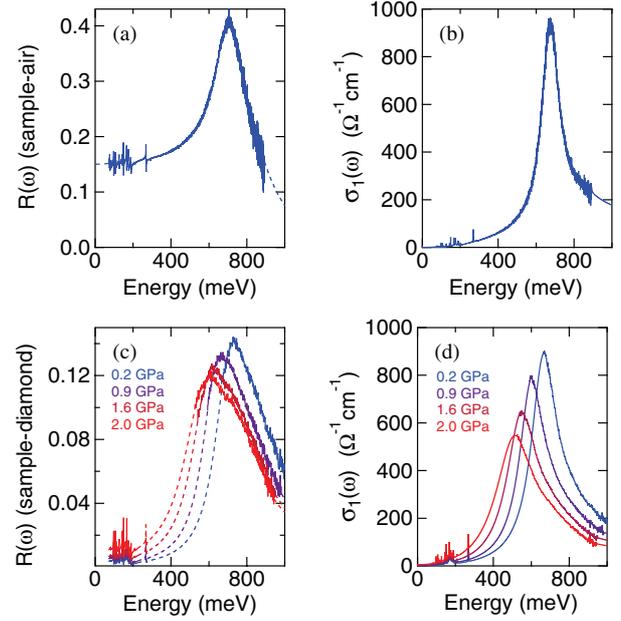


FIG. 1 (color online). (a) Static reflectivity at ambient pressure of the ET-F<sub>2</sub>TCNQ, measured with the electric field parallel to the  $a$  axis. (b) Real part of the optical conductivity  $\sigma_1(\omega)$  at ambient pressure. (c) Steady state reflectivity of the ET-F<sub>2</sub>TCNQ along the  $a$  axis for selected pressures. (d) Pressure dependence of the optical conductivity  $\sigma_1(\omega)$ .

Eq. (1). The onsite repulsion  $U$  was assumed to be a constant 845 meV at all pressures. The large Mott gap of ET-F<sub>2</sub>TCNQ enables a  $1/U$  strong coupling expansion of the extended Hubbard model giving a reduced optical conductivity  $\omega\sigma_1(\omega)$  in the form

$$\omega\sigma_1(\omega) = g_0 t^2 e^2 \left\{ \Theta(V - 2t) \pi \left[ 1 - \left( \frac{2t}{V} \right)^2 \right] \delta(\omega - \omega_{CT}) + \Theta(4t - |\omega - U|) \frac{2t \sqrt{1 - \left( \frac{\omega - U}{4t} \right)^2}}{V(\omega - \omega_{CT})} \right\} \quad (2)$$

where  $e$  is the electronic charge,  $\Theta$  is the Heaviside function and  $g_0 = 2.65$  is the zero-momentum form factor accounting for the spin degrees of freedom [15,16] (see Supplemental Material [11]).

This analytical result highlights the two dominant contributions to  $\omega\sigma_1(\omega)$  resulting from the relevant quasiparticles of this system. The first is a delta peak located at  $\omega_{CT} = U - V - 4t^2/V$ , and corresponds to a Mott-Hubbard exciton composed of a bound holon-doublon (HD) pair. A second broad peak is centered around  $U$ , with a bandwidth of  $8t$ , and corresponds to the continuum of states associated with unbound particle-hole (PH) excitations [15,16]. These two types of excitations are visualized for the 1D lattice model in Fig. 2(d). As pressure

is applied, the exciton peak shifts to the red, whereas the continuum remains centered at  $U$  and broadens with the increase in bandwidth.

A comparison of the measured and fitted  $\omega\sigma_1(\omega)$ , normalized to the peak value of the spectrum measured at ambient pressure, is reported for three selected pressures in Figs. 2(a)–(c) as black (measured data) and gray (theory fits) curves. The fit has been performed here after subtraction of the low-frequency tail of the intramolecular absorption bands near 3.5 eV [4,5]. The fitted values for  $t$  and  $V$  are summarized in Fig. 2(e). The nearest neighbor interaction  $V$  and the hopping amplitude  $t$  are both observed to increase with pressure, from 120 to 203 meV and from 40 to 85 meV, respectively.

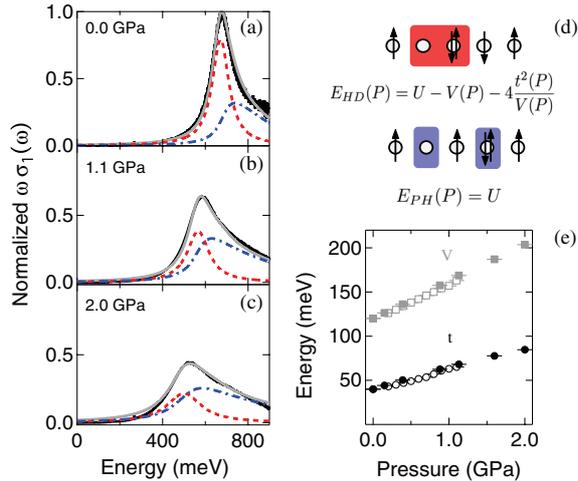


FIG. 2 (color online). (a)–(c) Normalized reduced optical conductivity for selected pressures (black solid line), with corresponding fit (gray solid line). The contributions of the holon-doublon pair (red dashed line) and of the particle-hole continuum (blue dashed-dotted line) are shown below the curves. (d) Sketch of a holon-doublon pair (top) and of a typical particle-hole continuum excitation (bottom). (e) Pressure dependence of the extended Hubbard model parameters  $V$  (squares) and  $t$  (circles) extracted from the fit of the steady state  $\omega \sigma_1(\omega)$ .  $U$  is kept fixed to 845 meV. Filled and empty symbols identify distinct experimental runs.

Optical pump-probe experiments were then used to measure the ultrafast recombination after prompt photoexcitation of holon-doublon pairs. An amplified Ti:sapphire laser, operating at a 1 kHz repetition rate and generating 800-nm-wavelength pulses, was used to drive a near infrared optical parametric amplifier, which was used for degenerate pump-probe experiments ( $\lambda_{\text{pump}} = \lambda_{\text{probe}}$ ) in a diamond anvil cell.

In a first series of experiments, the 100 fs pulses were tuned between 1.6 and 2.2  $\mu\text{m}$  wavelengths, to track the peak of the conductivity at each pressure value (see Fig. 2) and thus excite bound holon-doublon pairs. Above 1.3 GPa the tuning was no longer possible, as for higher pressures the laser spectrum overlapped with the multiphonon absorption in the diamond anvil.

A second set of experiments was performed with pump and probe wavelengths fixed on the center of the pressure-independent particle-hole continuum band (740 meV, 1.7  $\mu\text{m}$  wavelength). Both experiments were performed with a pump fluence of 300  $\mu\text{J}/\text{cm}^2$ , in a regime in which the excitation of holon-doublon pairs is sparse and the signal scales linearly with the number of absorbed photons.

In Fig. 3, the normalized time-resolved reflectivity changes  $\Delta R/R$  are reported on a semilogarithmic scale [see panels (a) and (c)]. In both cases, photoexcitation promptly reduced the holon-doublon band and the particle hole continuum, with a drop in reflectivity  $\Delta R/R \sim -1\%$ , followed by a rapid recovery of the signal with a double exponential law [4,6]. Only the fast time constant showed pressure dependence, with the recombination rate decreasing at a rate of 116 fs/GPa (490

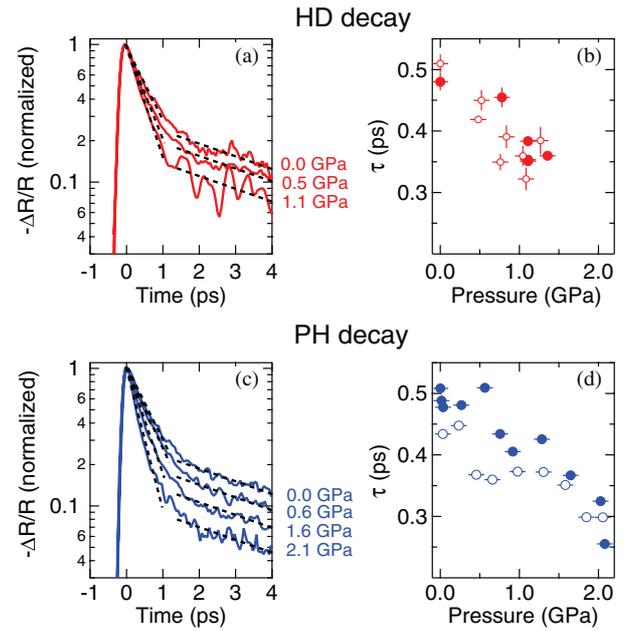


FIG. 3 (color online). (a) Normalized  $\Delta R/R$  time domain curves on the holon-doublon pair peak (HD) for selected pressures (solid lines). Black dashed lines are guides to the eye showing the biexponential decay, linear on a log scale. (b) Holon-doublon recombination lifetimes extracted from a fit to the data. Filled and empty symbols identify distinct experimental runs. (c) Normalized  $\Delta R/R$  time domain curves on the particle-hole continuum peak (PH) for selected pressures (solid lines). Black dashed lines are guides to the eyes showing the biexponential decay. (d) Particle-hole continuum recombination lifetimes extracted from a fit to the data. Filled and empty symbols identify distinct experimental runs.

to 350 fs between 0 and 1.3 GPa) for bound holon-doublon pairs and 85 fs/GPa (470 to 300 fs between 0 and 2 GPa) for the particle hole continuum. Both holon-doublon and particle-hole excitations exhibited similar recombination times and similar dependence on pressure. Indeed, from the static fitting discussed above, the ratio  $V/t$  is reduced from  $V/t \sim 3.0$  to  $V/t \sim 2.4$ , close to the critical ratio  $V/t \sim 2$  for which the exciton peak cannot be isolated from the continuum [15,16]. The slow time constant of 2.5 ps, interpreted here as resulting from the thermalization of high-energy molecular modes heated by the recombination of quasiparticles, was independent on pressure.

To analyze this pressure dependence quantitatively, we first note that recombination of bound holon-doublon pairs (or disassociated pairs throughout the particle hole continuum) must involve dissipation of an excess energy of order  $U - V$  by coupling to a bath. In the absence of such a bath the only possible decay paths involve kinetic energy transfer (creation of particle-hole pairs) or spin excitations within the Hubbard model itself, where the relevant energy scales are the bandwidth  $t$  and the exchange coupling  $t^2/(U - V)$ , respectively [17]. For  $U \gg V$ ,  $t$  a large number of scattering events is required for

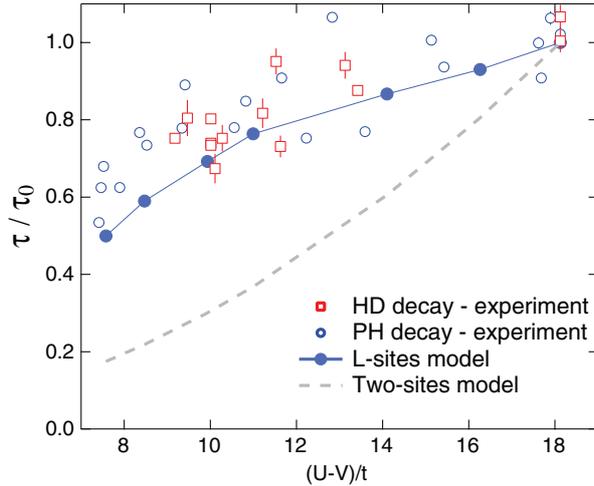


FIG. 4 (color online). Experimental relaxation times (empty symbols) for both HD and PH resonant excitation normalized to their ambient pressure values  $\tau_0$  and shown as a function of  $(U-V)/t$ . The calculated holon-doublon lifetimes (filled circles) found from solving an  $L$ -site effective model (see Fig. 5) with spin-boson scaling for the bare decay rate. For comparison the  $L = 1$  dimer result is shown (dashed line).

recombination, leading to a decay rate that is exponentially small with  $U/t$  [17–20]. Owing to the weak electron-phonon coupling in ET-F<sub>2</sub>TCNQ [5], and lack of efficient radiative emission, it is reasonable to assume that high-frequency molecular modes are the primary scattering partner for the rapid decay of hot quasiparticles observed in our experiment.

In the following discussion, we assume that recombination occurs locally and the density of holon-doublon excitations is sufficiently low that only a single pair need be considered. This is substantiated by the measured fluence dependence. In the range explored in our experiments the signal scaled linearly with the laser fluence, while recombination rates were found to be independent of it. This behavior suggests that excitations are sparsely distributed and recombination is localized.

The simplest possible model involves a dimer of ET molecules coupled to a continuum of bosonic modes, as is commonly used to model dissipative electron transfer [21,22]. The holon-doublon and singly occupied configurations of the dimer, with an energy gap  $U-V$  and tunneling  $t$  between them, comprise a two-level system of the spin-boson model [23]. We take a super-Ohmic form for spectral function  $\mathcal{J}(\omega)$  appropriate for electron-phonon interactions [24]. Moreover, given  $U-V \gg t$ , the system is in the large-bias regime where the far-off-resonant tunneling mediates the decay of the holon-doublon pair by dissipating the large energy gap into the bosonic reservoir. The rate of decay  $\Gamma$  in this limit is proportional to  $t^2/(U-V)^2 \mathcal{J}(U-V)$  [23]. As the dominant contributions to the spectral function at the energy gap  $\mathcal{J}(U-V)$  arise from local vibrational modes it is assumed to be independent of pressure. This then gives a scaling of  $\Gamma$  with

the pressure dependent microscopic parameters as  $t^2/(U-V)^2$ , which sensibly predicts an increase with  $t$  and a decrease with  $U-V$ .

In Fig. 4 the experimentally measured holon-doublon and particle-hole continuum decay rates, normalized to the ambient pressure decay rate  $1/\tau_0$ , are plotted as a function of  $(U-V)/t$ . The dashed line shows the predicted change in the recombination rate (see Supplemental Material [11] for details), consisting of a more than fivefold increase at the largest pressure. Thus, the two-site model on its own does not reproduce the experimentally measured trend.

We note that previous time-resolved spectroscopy experiments showed that at least three sites are necessary to account for the photoresponse [4], owing to the possibility for bound holon-doublon pairs next to a singly occupied site  $|\dots_0\uparrow\_ \dots\rangle$  to tunnel into a configuration of the type  $|\dots_0\uparrow\_ \dots\rangle$ , where  $|\dots_0\dots\rangle$  represents a holon,  $|\dots\uparrow\dots\rangle$  a doublon, and  $|\dots\dots\rangle$  represents a singly occupied site of either spin. This separation occurs at a rate determined by the hopping amplitude  $t$  and is limited by a barrier  $V$ , where both of these increase with pressure. Importantly, the configuration  $|\dots_0\uparrow\_ \dots\rangle$  has a lower probability to recombine than the configuration  $|\dots_0\uparrow\dots\rangle$ , as two hopping events are necessary.

To include this effect, we employed an effective model based on the sketch of Fig. 5, derivable from the strong-coupling limit (see Supplemental Material [11]), where in addition to the singly-occupied configuration  $|g\rangle$  and adjacent holon-doublon pair  $|0\rangle$ , other states  $|l\rangle$ , representing holon and doublons separated by  $l$  sites were considered, up to maximum distance  $L$ . The potential energy of the model then

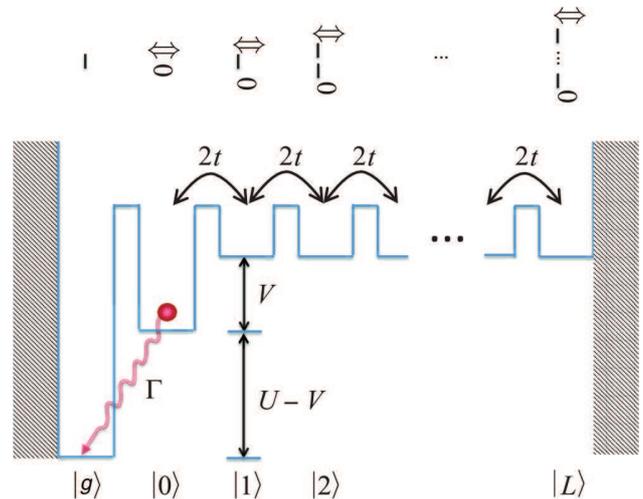


FIG. 5 (color online). Effective model describing holon-doublon dynamics in the strong-coupling limit. The state  $|g\rangle$  is the ground state containing no holons or doublons, whereas the state  $|0\rangle$  represents an adjacent (zero separation) holon-doublon pair. The remaining states  $|l\rangle$  represent the holon and doublon being separated by  $l$  sites. In the limit  $L \rightarrow \infty$  these unbound states form the particle-hole continuum. The relaxation to  $|g\rangle$  at a bare spin-boson rate  $\Gamma$  only occurs locally from state  $|0\rangle$ .

mimicked the interactions of the equivalent many-body configurations in the full, extended Hubbard model. Importantly, the optical conductivity of this effective model, when  $L \rightarrow \infty$ , exactly reproduces that of Eq. (2) for the extended Hubbard model (see Supplemental Material [11]).

Local recombination was added to this effective model via a Markovian quantum dissipation process, appropriate for the super-Ohmic large-bias limit [25] (see Supplemental Material [11]), that incoherently drives only the transition  $|0\rangle \rightarrow |g\rangle$  at a bare rate  $\Gamma$ . This effective model reveals that even the addition of one ionized holon-doublon state  $|1\rangle$  which is unaffected by the decay, i.e., taking  $L = 1$ , causes the suppression of the actual decay rate  $\Gamma_{\text{eff}}$  to  $|g\rangle$  from the bare rate  $\Gamma$  as

$$\Gamma_{\text{eff}} = \frac{\Gamma}{2} \left( 1 + \frac{V}{\sqrt{V^2 + 16t^2}} \right). \quad (3)$$

We applied this effective model by first fitting the bare rate  $\Gamma$  to reproduce the observed zero pressure decay rate. For all other pressures  $\Gamma$  was increased according to the spin-boson scaling by using the values for  $t$ ,  $V$  reported in Fig. 2(e). The effective decay rate  $\Gamma_{\text{eff}}$  was then calculated numerically from this model for different sizes  $L$ . As  $L$  increases the suppression of  $\Gamma_{\text{eff}}$  becomes more pronounced since the disassociated holon-doublon pair can ballistically separate to larger distances remaining immune to the local decay. Thus, we find that coherent dynamics on more than two sites, accounting for the break-up of the holon-doublon pair, competes and slows down the recombination caused by the local decay process.

In conclusion, we have experimentally investigated the pressure dependence of hot quasiparticle recombination in a one dimensional Mott insulator. By fitting the steady state infrared properties with a model based on the extended Hubbard Hamiltonian, we extracted the pressure dependence of the Hubbard parameters  $t$  and  $V$  up to 2.0 GPa, and correlated them to the recombination rates. A key inference made by comparing the experimentally determined dependence to theory is that the decay of quasiparticles is likely connected to the coherent evolution of holon-doublon pairs immediately after excitation. Based on this idea, it may be possible in the future to accelerate or decelerate the photoinduced dynamics of correlated electron systems by pulse shaping and by coherent optical control techniques. Such ability would have interesting ramifications in both fundamental science and applications.

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